Hello rising algebra 2 students!

It's time for summer math! We would like to make sure that you continue to learn this summer by completing the following algebra math topics. Research shows that all students experience learning losses during the summer when they do not engage in educational activities. On average, students lose approximately 2.6 months of grade level equivalency in mathematical computations during the summer months (Harvard Graduate School of Education).

At the beginning of each topic, there are example problems to refresh your memory. If you're still stuck, I highly recommend Khan Academy as a resource.

Please turn in your completed summer math assignment to your algebra 2 teacher on the first day of school to receive extra credit!

Wishing you a safe and relaxing summer! Mrs. Boulet

Combining Like Terms

Example: Simplify
$$8x^2 + 16xy - 3x^2 + 3xy - 3x$$

 $8x^2 - 3x^2 + 16xy + 3xy - 3x$ Identify &/or Group Like Terms
 $5x^2 - 3x + 19xy$

Simplify

6x + 11y - 4x + y	-3p - 4t - 5t - 2p	3x²y - 5xy ^y + 6x²y
-5m + 3q + 4m - q	9x - 22y + 18x - 3y	$5x^2 + 2xy - 7x^2 + xy$

Solving Equations with variables on both sides

Example:	Solve	6a - 12 = 5a + 9		
		a - 12 = 9	subtract 5a from both sid	des
Solve each equ	uation	a = 21	add 12 to both sides	
	3x + 5 = 2x + 11		8m + 1 = 7m - 9	11q - 6 = 3q + 8q
	-14 + 3a = 10 - a		-2t + 10 = -t	-7x + 7 = 2x - 11

Literal Equations

	Solve $2p = kx - q$ for x	
	2p = kx - q	Solve for x by isolating the variable x
	2p + q = kx	Add q to each side
	$\frac{2p+q}{k} = \chi$	Divide each side by k
Solve for the indicated variable.	$\chi = \frac{2p+q}{k}$	
ax - c = b; solve for x	2x + 4y = 8; solve for y	$2/_{3}y + 4x = -2$; solve for y

Solving Inequalities & Graphing





-x + 2 > 7	- 5 + m ≤ 4	z + 6 > - 2
-16 - 8x ≥ 0	x - 5 < 4	-3x + 4 ≤ -5
8x - 6 ≥ 10	9(2x - 5) - 3 < 7x - 4	9x - 11 > 6x - 9

Calculating Slope

Example:

Find the slope of a line passing through (3, -9) and (2, -1).

	$m = \frac{y_2 - y_1}{x_2 - x_1}$	Formu	la for slope
	$m = \frac{-1 - (-9)}{2 - 3} = \frac{-1 + 9}{-1}$	Substi	tute values and simplify
Find slope.	$m = \frac{8}{-1} = -8$	Slope	is -8
(4 , 1) (3, 6)	(5, 6) (9, 8)		(-1, 7) (-3, 18)
(-8, 0) (5, -2)	(0, - 4) (7, 3)		(-6, -4) (1, 10)

Finding the equation of a line (given a point and y-intercept)

Example Find an equation of the line that passes through the point (3,4) and has a y-intercept of 5

	y = mx + b Slope-intercept 4 = 3m + 5 Substitute 5 for		form	
			Substitute 5 for b, 3 for x, and 4 for y.	
	-1 = 3m		Subtract 5 from both sides	
	-⅓ = m		Divide each side	e by 5
Find the equation of the line.	y = -1/3 x	x + 5	With slope -1/3	& y-intercept of 5, this is the line's equation
(2,1); b = 5		(7, 0); b = 13		(-5, 3); b = -12
(-3, -3); b = -2		(-3, 10); b = 8		(-1, 4); b = -8

Finding the equation of a line (given a point and the slope)

Example Find an equation of the line that passes through the point (1,2) and has a slope of -3

$y - y_1 = m(x - x_1)$	Point-Slope Form
y - 2 = -3(x - 1)	Substitute 2 for y_1 1 for x_1 and -3 for m
y - 2 = -3x + 3	Distribute the -2
y = -3x + 5	Add 2 to both sides

Find the equation of the line in slope-intercept form.

(2,3); m = -4	(-1, 5); m = 2	(4, 6); m = -½
(-3, - 4); m = ⅔	(0, 4); m = -3/2	(5, 0); m = -4

Finding the equation of a line (given two points)

Example

Write an equation of the line that passes through the points (4,8) and (3,1).

-	
$m = \frac{1-8}{3-4}$	Substitute values into the formula for slope
$m = \frac{-7}{-1} = 7$	Simplify
<i>y-1 = 7(x - 3)</i>	Select either point and substitute values of point and slope into point-slope form
<i>y-1 = 7x -21</i>	Distribute the 7
y = 7x - 20	Add 1 to each side to get the equation of a line in slope-intercept form

Find the equation of the line in slope-intercept form.

(6, -3) (1, 2)	(5, -1) (4, -5)	(-3, -7) (0, 8)
(-7, 9) (-5, 3)	(-2, 4) (3, -6)	(1, 2) (-1, -4)

Standard Form of a Line (Ax + By = C)

Example	Graph a line in standard form 2x+3y = 6		
Option 1:	Change to slope-intercept form	Option 2	Keep in Standard form
2x + 3y = 6 3y = -2x + 6 $y = -\frac{2}{3}x + 2$ $m = -\frac{2}{3}$ and $b = 1$	Subtract 2x from each side Divide everything by 3 Graph a y-intercept at 2 & a Slope of -¾	2x + 3y = 6 $m = \frac{-A}{B} = \frac{-2}{3}$ $b = \frac{C}{B} = \frac{6}{3} = 2$	Slope in standard form $\frac{-A}{B}$ y-intercept in stand form $b = \frac{C}{B}$ Graph using a slope of $-\frac{2}{3}$ & y-intercept of 2

Graph the y-intercept of 2, then go down 2 and right 3 to find another point on the line.

You can also go up 2 and left 3; connect the points to make a line.



Graph the equation of each⁴line.



Solving Systems of Equations (by graphing or substitution)

Example Solve the system y = 2x + 5 and $y = -\frac{1}{2}x - 4$



Solve each system by graphing or substitution



Solve Systems of Equations (by elimination)

Example	x - y = 4 $(x - y = 4)$		2x - 2y = 8	
	2x + 2y = -4	2x + 2y = -4	2x + 2y = -8	
	Given	Multiply by 2 to eliminate the y	4x = 0	Add the 2 equation
			x = 0	Divide each side by 4
			2(0) + 2y = -4	Substitute 0 for x in
			2y = -4	either equation; simplify
			y = -2	Divide each side by 2
			(0, -2)	Solution to system

Solve each system by elimination.

x - y = 1	3x + 4y = 19	2x - 3y = 9
x + y = 3	3x + 6y = 33	-5x - 3y = 30
5x - y = -6 -x + y = 2	6x- 3y = 6 6x +8y = -16	The sum of two numbers is 28. Their difference is 4. What are the two numbers?

Solving Proportions

Example

$\frac{x}{8} = \frac{3}{4}$	
4x = 8·3	Cross multiply
4x = 24	
x = 6	

$\frac{6}{x+4} = \frac{2}{9}$	
$6 \cdot 9 = 2(x + 4)$	Cross Multiply
54 = 2x + 8	Simplify both sides
46 = 2x	Subtract 8 from both sides
x = 23	Divide each side by 2

Solve each proportion to find the value of the given variable.

$\frac{y}{40} = \frac{3}{8}$	$\frac{3}{p-6} = \frac{1}{p}$	$\frac{3}{8} = \frac{3}{2d}$
$\frac{r}{3r+1} = \frac{2}{3}$	$\frac{3}{m+4} = \frac{9}{14}$	$\frac{w}{4} = \frac{9}{w}$

Property of Exponents

Property		Example
Product of Powers	$a^{m} \cdot a^{n} = a^{m+n}$	$x^4 \cdot x^2 = x^6$
Power of a Power	(a ^m) ⁿ = a ^{m · n}	$(x^4)^2 = x^8$
Power of a Product	(ab) ^m = a ^m b ^m	$(2x)^3 = 8x^3$
Negative Power	$a^{-n} = \frac{1}{a^n}$	$\chi^{-3} = \frac{1}{x^3}$
Zero Power	a ⁰ = 1	4 [°] = 1
Quotient of Powers	$\frac{a^m}{a^n} = a^{m-n}$	$\frac{x^{10}}{x^4} = x^6$
Power of Quotients	$\left(\frac{a}{b}\right)^m = \frac{a^m}{b^m}$	$\left(\frac{x}{y}\right)^3 = \frac{a^3}{b^3}$

Simplify each exponent. Answers should be written using positive exponents.

$g^5 \cdot g^{11}$	(b ⁶) ³	w ⁻⁷
$\frac{y^{12}}{y^8}$	(3x ⁷)(-5x ³)	$(-4a^5b^0c)^2$
-6(x ² y ³) ⁴	(-18mn ⁴)(-% mn ²)	$\frac{16x^5y^2}{2x^3y^3}$

Polynomial Operations

Add or Subtract like terms	Distributing	Multiplying binomials &/or trinomials
(7x ² + 4x - 3) - (-5x ² - 3x + 2) 7x ² -(-5x ²) + 4x - (-3x) -3-(2) 12x ² + 7x - 5	-2x(5x + 11) -10x ² - 22x	$(7x - 3)(3x + 7)$ Multiply everything in the 1st binomial times the 2nd $7x \cdot 3x + 7x \cdot 7 - 3 \cdot 3x - 3 \cdot 7$ First-Outside-Inside-Last (FOIL) $21x^2 + 49x - 9x - 21$ Simplify $21x^2 + 40x - 21$ Combine like terms

Simplify each polynomial

(2x +3y) + (4x + 9y)	$(7x^2 + x + 1) - (3x^2 - 4x - 3)$	(7a ² - a + 4) - (3a ² - 4a - 3)
-3x(8x ² - 3x + 1)	-10pq(3pq + 4p - 5q ²)	5w(w ² -7w + 3) -2w(2w ² -5w + 2)
(x + 4)(x - 7)	(5x - 2y)(3x + 9y)	(z + 5)(4z - 6)

Factoring Polynomials $(ax^2 + bx + c)$

Examples:

Factoring out GCF	Difference of squares	Perfect Square Trinomials	Trinomials
$6x^2 + 21x$	x ² - 64	$4x^2 + 12x + 9$	$3x^2 + 7x + 2$
3x(2x + 7)	(x + 8)(x - 8)	$(2x + 3)^2$	(3x + 1)(x + 2)

Factor completely.

6e ³ f - 11ef	y² - 5y - 84	$6x^2 + 7x + 2$
6z ² - 5z - 4	75x ² - 147y ²	x ² - 25
x ² - 6x + 9	$16c^2 + 72cd + 81d^2$	x ⁴ - 16

Solving Quadratics

Example

$x^{2} + 3x^{2} = 10$	
$x^2 + 3x^2 - 10 = 0$	Subtract 10 from both sides so the quadratic is equal to 0
(x - 5)(x + 2) = 0	Factor (see previous section on different kinds of factoring)
x - 5 = 0 and $x + 2 = 0$	Use Zero Product Property and put each binomial equal to O
x = 5 and $x = -2$	Solve both for x.

Solve each quadratic to find the possible values of x.

$3x^2 - 12 = 0$	$6x^2 - 5x + 1 = 0$	$x^2 + 7x = 18$
· ² ·1100	o ² 15	
x +11x = 80	$2x^{-} = x + 15$	$3x^{2} + 3x^{2} - 60x = 0$
x +11x = 80	2x ⁻ = x +15	3x" + 3x" -60x = 0

Distance Formula

Example:

Find the distance between the points (-4,3) and (-7,8)

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$d = \sqrt{(-7 - -4)^2 + (8 - 3)^2}$$

$$d = \sqrt{(-3)^2 + (5)^2}$$

$$d = \sqrt{9 + 25}$$

$$d = \sqrt{34}$$

Distance formula

Substitute the coordinates into the distance formula

Simplify each parentheses

Simplify by squaring each

Combine like terms and make sure it is in simplest radical form.

Find the distance between each pair of points

(3, 6) (0, -2)	(-3, 4) (1, 4)	(8, -2), (-3, -6)
(5, -2) (-6, 5)	(-6, -6) (-3, 2)	(-8, 5) (-1, 1)